## Computer Science 4602 Fall 2020 <br> Quiz 2

Answer all of the questions. Check your work.

1. Draw a state transition diagram of a FSM that decides language $A=$ $\{" a b "\}$ over alphabet $\{a, b\}$. There is only one string in language $A$. Be sure to mark the start state and accepting states. Be sure there is a transition out of every state for every symbol in the alphabet.
2. Draw a state transition diagram of a FSM that decides language $B=$ $\left\{x \in\{a, b\}^{*}| | x \mid \geq 2\right.$ and the next to last symbol of $x$ is $\left.a\right\}$. Some of the strings in $B$ are " $a a$ ", "bab", "bbaab" and "abaaa". Be sure to mark the start state and accepting states.

Hint. Have a state for each pair of symbols that might be the last two in a string. The state for strings ending on $b b$ can serve as a start state.
3. Prove that language $C=\left\{a^{n} b^{2 n} \mid n>0\right\}$ over alphabet $\{a, b\}$ is not regular. Make your proof clear and readable, but not verbose. Do not expect the reader to guess what you are doing.

